

Key Notes

Chapter 9

Areas of Parallelograms and Triangles

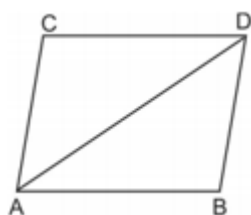
1. Figures on the same Base and Between the same Parallels
2. Parallelograms on the same Base and between the same Parallels
3. Triangles on the same Base and between the same Parallels

- Area of a figure is a number (in square unit) associated with the part of the plane enclosed by that figure.
- Two congruent figures have equal areas but the converse is not true.
- Area of a parallelogram = (base \times height)
- Area of a triangle = $\frac{1}{2} \times \text{base} \times \text{height}$
- Area of a trapezium = $\frac{1}{2} \times (\text{sum of parallel sides}) \times \text{height}$
- Area of rhombus = $\frac{1}{2} \times \text{product of diagonals}$
- Parallelogram on the same base and between the same parallels are equal in area.
- A parallelogram and a rectangle on the same base and between the same parallels are equal in area.
- Triangles on the same base and between the same parallels are equal in area.
- If a triangle and parallelogram are on the same base and between the same parallels, then.

$$(\text{Area of triangle}) = \frac{1}{2} (\text{Area of parallelogram})$$

- A diagonal of parallelogram divides it into two triangles of equal areas.

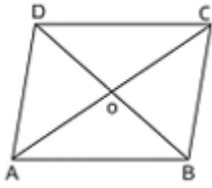
In parallelogram ABCD, we have Area of $\triangle ABD$ = area of $\triangle ACD$



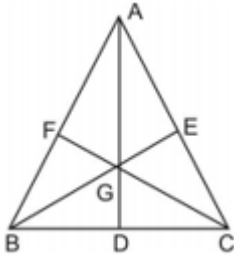
- The diagonals of a parallelogram divide it into four triangles of equal areas therefore

$$\text{ar}(\triangle AOB) = \text{ar}(\triangle COD) = \text{ar}(\triangle AOD) = \text{ar}(\triangle BOC)$$

Key Notes



- If a parallelogram and a triangle are on the same base and between the same parallel, then area of the triangle is equal to one half area of the parallelogram.
- A median AD of a $\triangle ABC$ divides it into two triangles of equal areas. Therefore $ar(\triangle ABD) = ar(\triangle ACD)$
- If the medians of a triangle intersect at G, then $ar(\triangle AGB) = ar(\triangle AGC) = ar(\triangle BGC) = \frac{1}{3} ar(\triangle ABC)$



- Triangles with equal bases and equal areas have equal corresponding altitude.